

**DYNAMICAL AND THERMAL EFFECTS OF NONLINEAR  
ACOUSTIC-GRAVITY WAVES IN THE UPPER ATMOSPHERE  
AT HIGH AND LOW SOLAR ACTIVITY.**

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- 1. Numerical wave model**
- 2. AGW surface sources**
- 3. Low and high solar activity**
- 4. AGW amplitudes**
- 5. Wave-induced heating and jets**
- 6. AGW thermal effect**
- 7. Conclusion**

# Main Equations

**The Equation of Continuity**

$$\frac{\partial \rho}{\partial t} + \frac{\partial (\rho v_\alpha)}{\partial x_\alpha} = 0;$$

**The Equations of Motion**

$$\frac{\partial \rho v_i}{\partial t} + \frac{\partial \rho v_i v_\alpha}{\partial x_\alpha} = -\frac{\partial p}{\partial x_i} - \rho g \delta_{i3} + \rho X_i + \frac{\partial \sigma_{i\alpha}}{\partial x_\alpha}; i, \alpha = 1, 2, 3$$

**The Equation of State of ideal gas**

$$p = \rho R T ;$$

**The Heat Balance Equation**

$$\frac{dp}{dt} = -\gamma p \operatorname{div}^r \mathbf{v} + (\gamma - 1) \frac{dQ}{dt},$$

$$\frac{dQ}{dt} = \rho (\varepsilon_t + \varepsilon_d + \varepsilon); \quad \rho \varepsilon_d = \sigma_{\alpha\beta} \frac{\partial v_\alpha}{\partial x_\beta}; \quad \rho \varepsilon_t = -\frac{\partial q_{m\alpha}}{\partial x_\alpha}.$$

# Molecular and Turbulent Viscosity and Heat Conduction

$$\sigma_{ij} = \mu \partial v_i / \partial x_j ,$$

$$q_i = -\kappa \partial T / \partial x_i .$$

**Coefficients  $\mu$  and  $\kappa$  take account of molecular and turbulent viscosity and heat conduction, respectively**

# Vertical Boundary Conditions

The upper boundary conditions at altitude  $h=500$  km

$$\left( \frac{\partial T'}{\partial z} \right)_{z=h} = 0, \quad \left( \frac{\partial u}{\partial z} \right)_{z=h} = 0, \quad (w)_{z=h} = 0$$

Lower boundary conditions at the Earth surface

$$(T')_{z=0} = 0, \quad (u)_{z=0} = 0,$$

$$(w)_{z=0} = a \sin[\sigma(t - x/c_x)],$$

The condition for  $w$  at the lower boundary is a source of waves in the model.

# Horizontal Boundary Conditions

Periodical conditions at horizontal boundaries

$$\alpha(x, z, t) = \alpha(x + L_x, z, t),$$

$$\alpha(y, z, t) = \alpha(y + L_y, z, t),$$

**Where**  $L_x = n \lambda_x; L_y = m \lambda_y;$

$$\lambda_x = \frac{2\pi}{k_x}; \lambda_y = \frac{2\pi}{k_y};$$

**are horizontal dimensions of atmospheric domain;**

**$k_x, k_y$  are horizontal wavenumbers.**

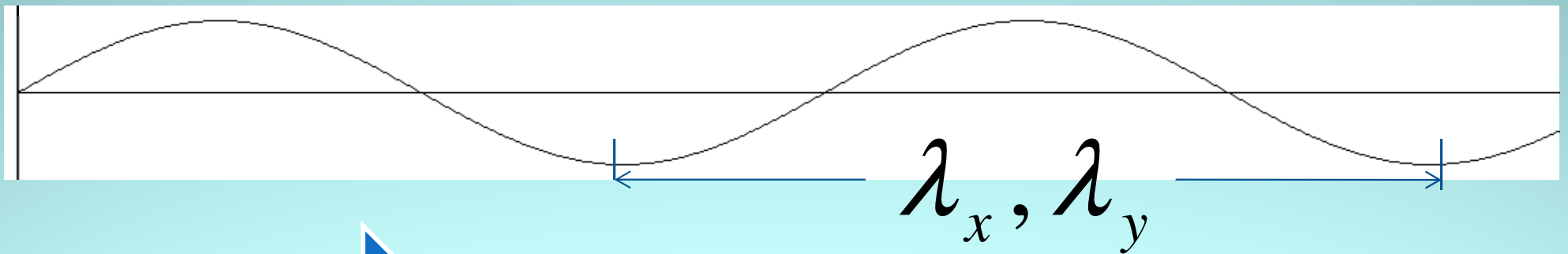
## **2. AGW surface sources**



# Plane Wave Excitation

$$w(x, y, z = 0, t) =$$

$$= W_0 \times \cos \left( \sigma \left( t - \frac{x}{c_x} - \frac{y}{c_y} \right) \right)$$



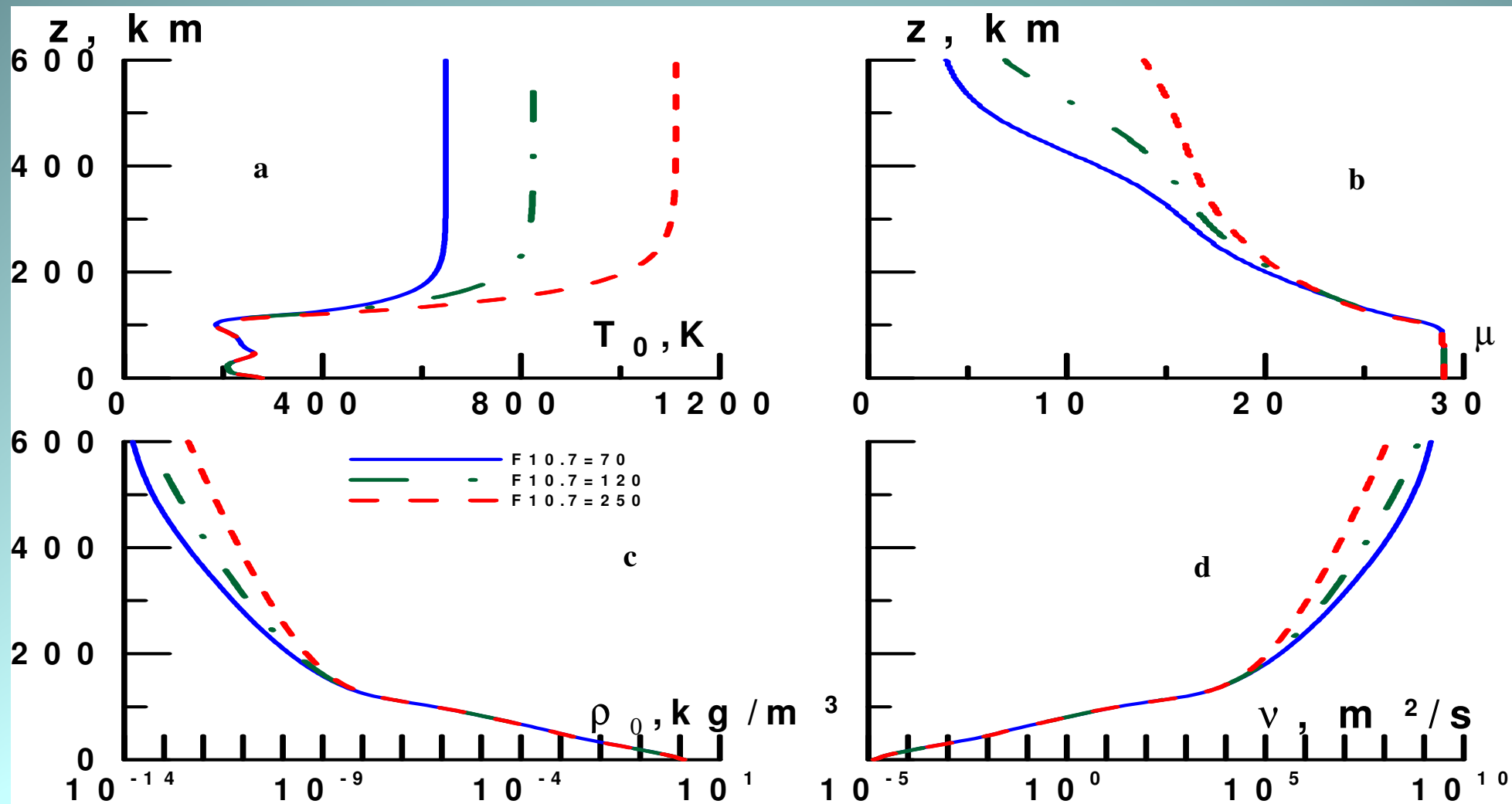
Phase velocity

$$c_i = \frac{\sigma}{k_i}; \quad k_i = \frac{2\pi}{\lambda_i}.$$



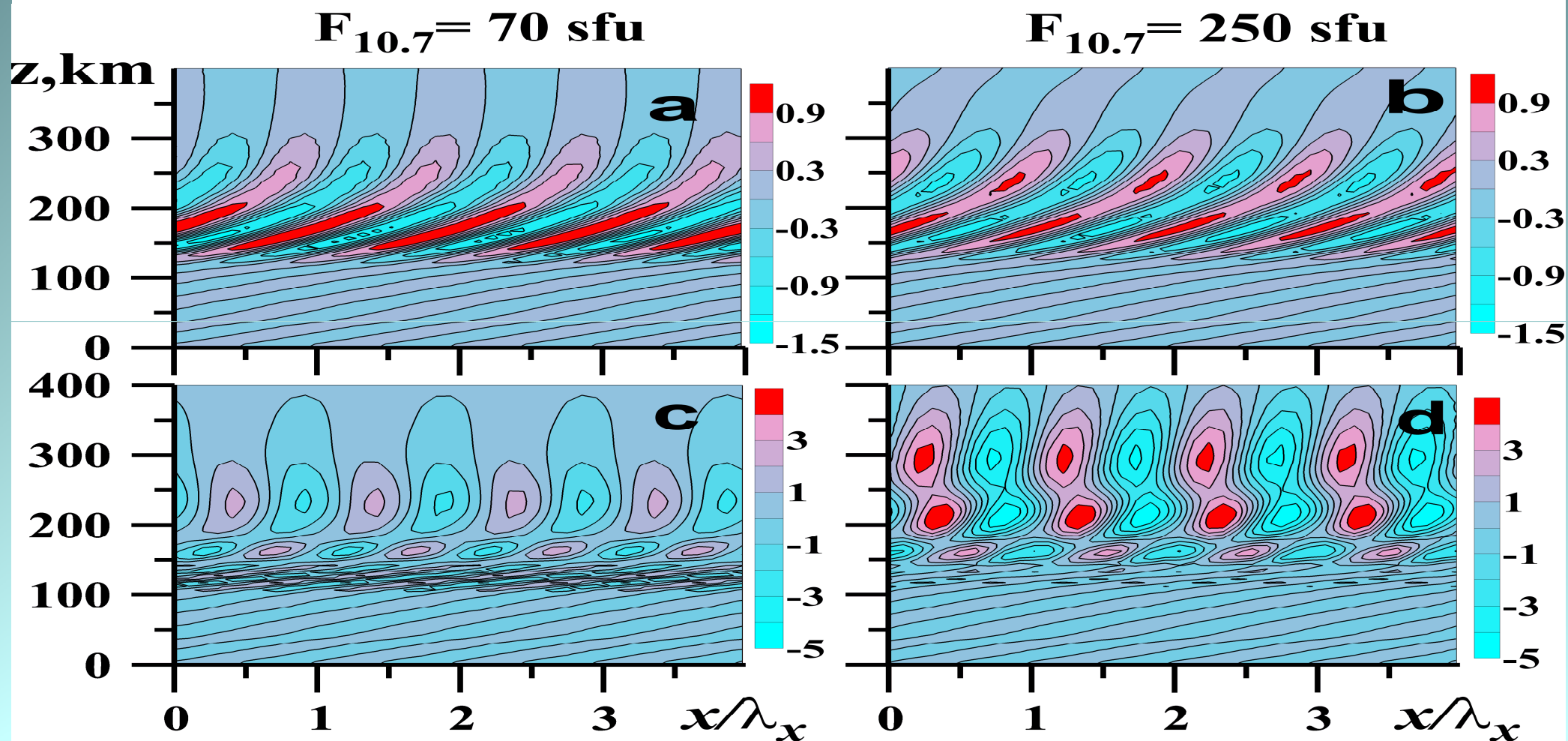
# **3. Low and high solar activity**

# Atmospheric parameters for different solar $F_{10.7}$ radiowave flux from the NRLMSISE-00 model



Background temperature (a), molecular weight (b), density (c) and kinematic viscosity (d)

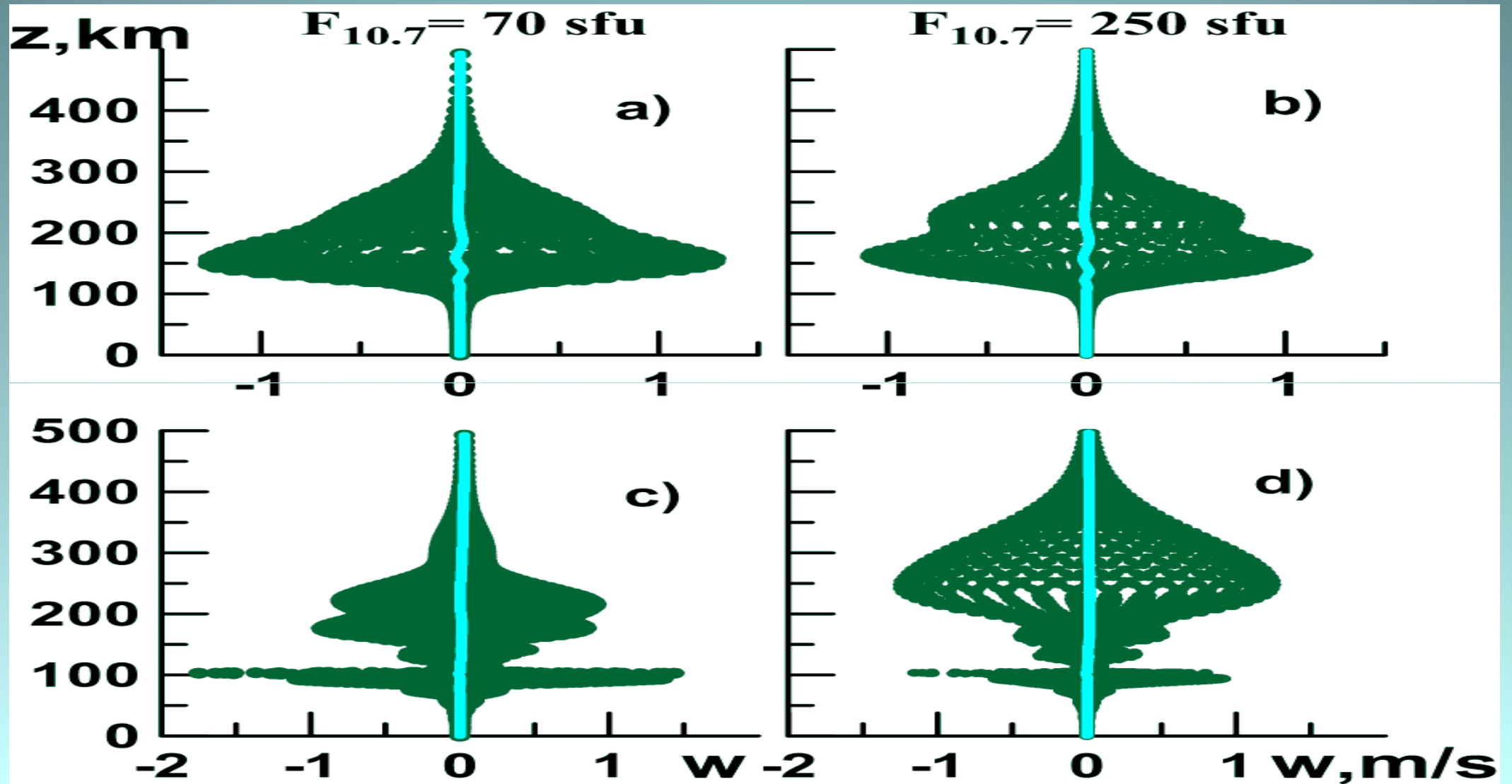
**Vertical velocity (in m/s) in the plane XOZ parallel to the horizontal wave vector at time  $t = 9\tau$  for values of solar radiowave flux**



**Wave source amplitudes  $W_0 = 0.1$  mm/s (a,b) and  $W_0 = 1$  mm/s (c,d), period  $\tau = 2 \times 10^3$  s and  $c_x = 100$  m/s and interval of wave activation  $t_0 = 1$  s**

# **4. AGW amplitudes at low and high solar activity**

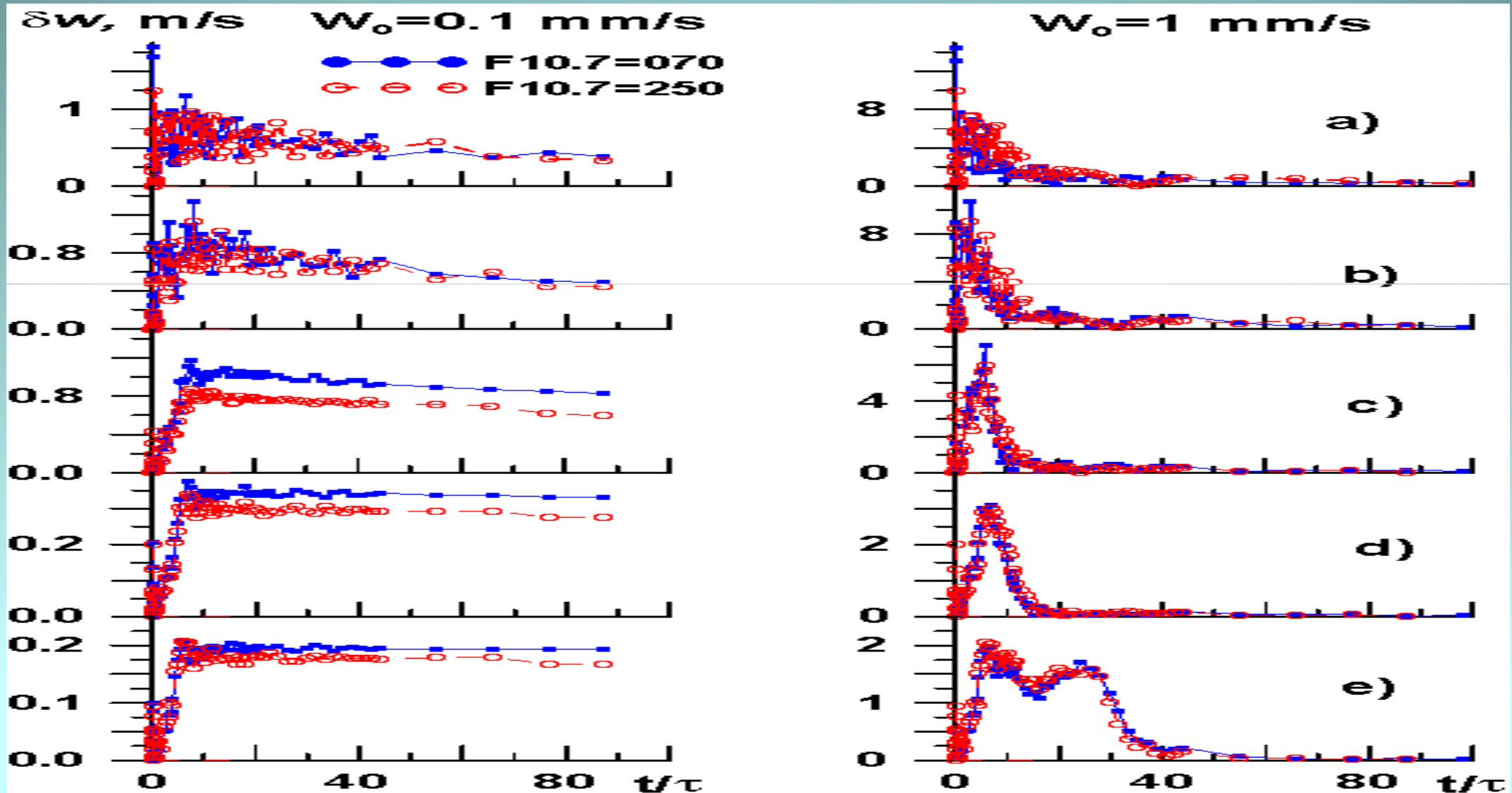
Vertical velocity perturbations from AGW source with period  $\tau = 2 \times 10^3$  s and  $c_x = 100$  m/s at time  $t = 55\tau$  for different solar radiowave flux



Source amplitudes  $W_0 = 0.1$  mm/s (a,b) and  $W_0 = 1$  mm/s (c,d).  
Thick lines show average values for each altitude.

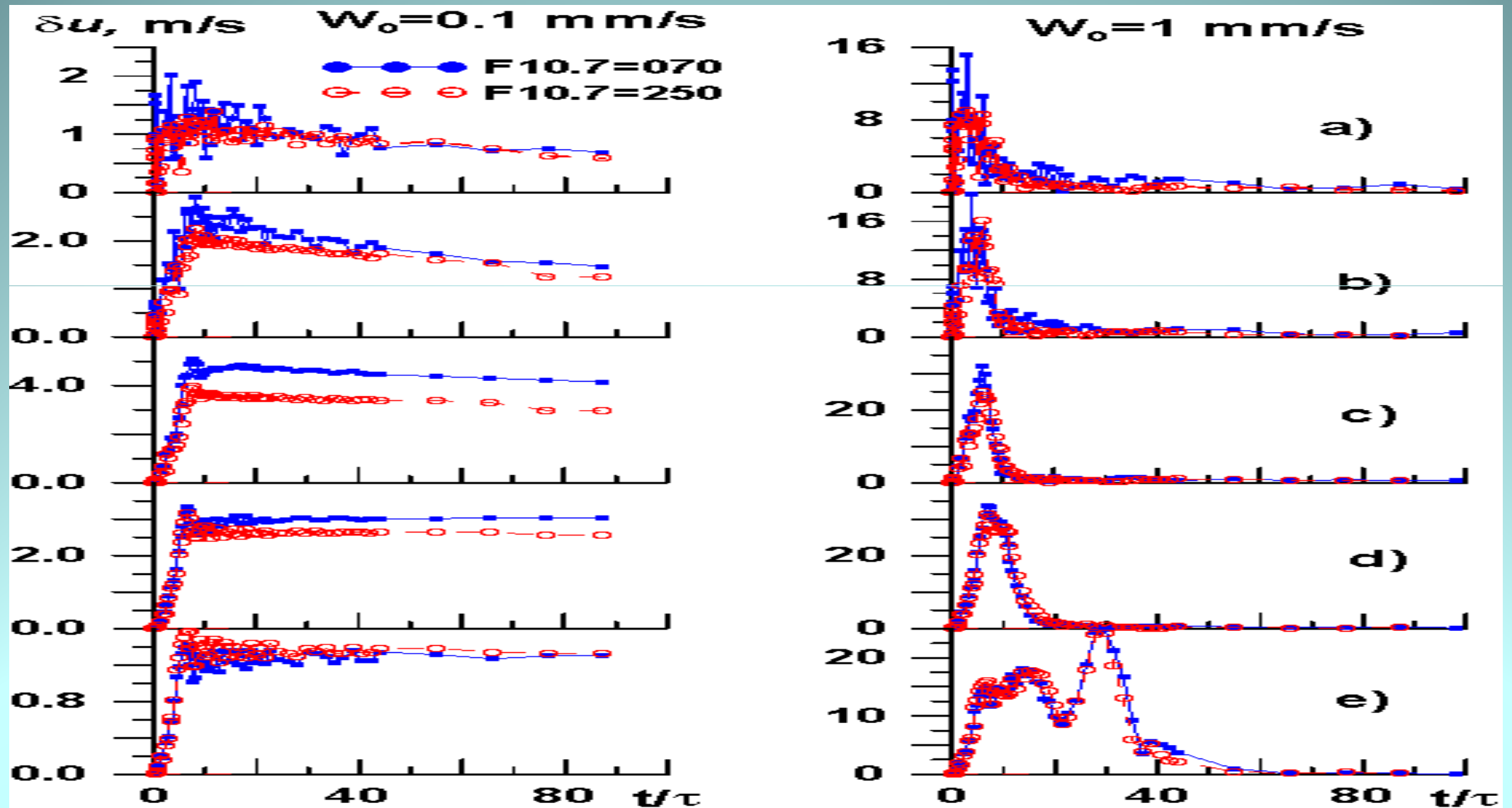
# Simulated standard deviation of vertical velocity

at  $Z = 250$  (a),  $200$  (b),  $150$  (c),  $120$  (d),  $110$  km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



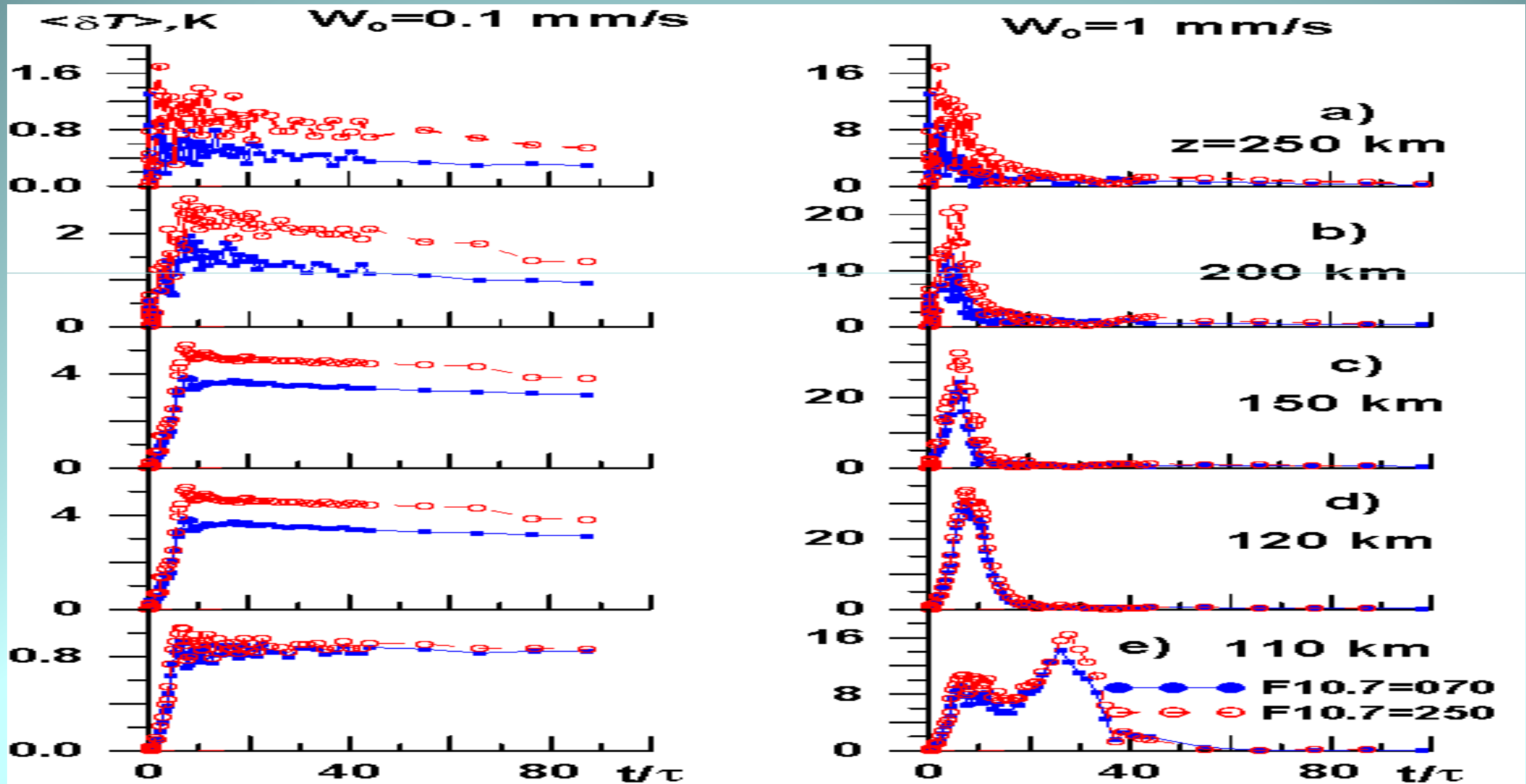
# Simulated standard deviation of horizontal velocity

at  $Z = 250$  (a),  $200$  (b),  $150$  (c),  $120$  (d),  $110$  km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



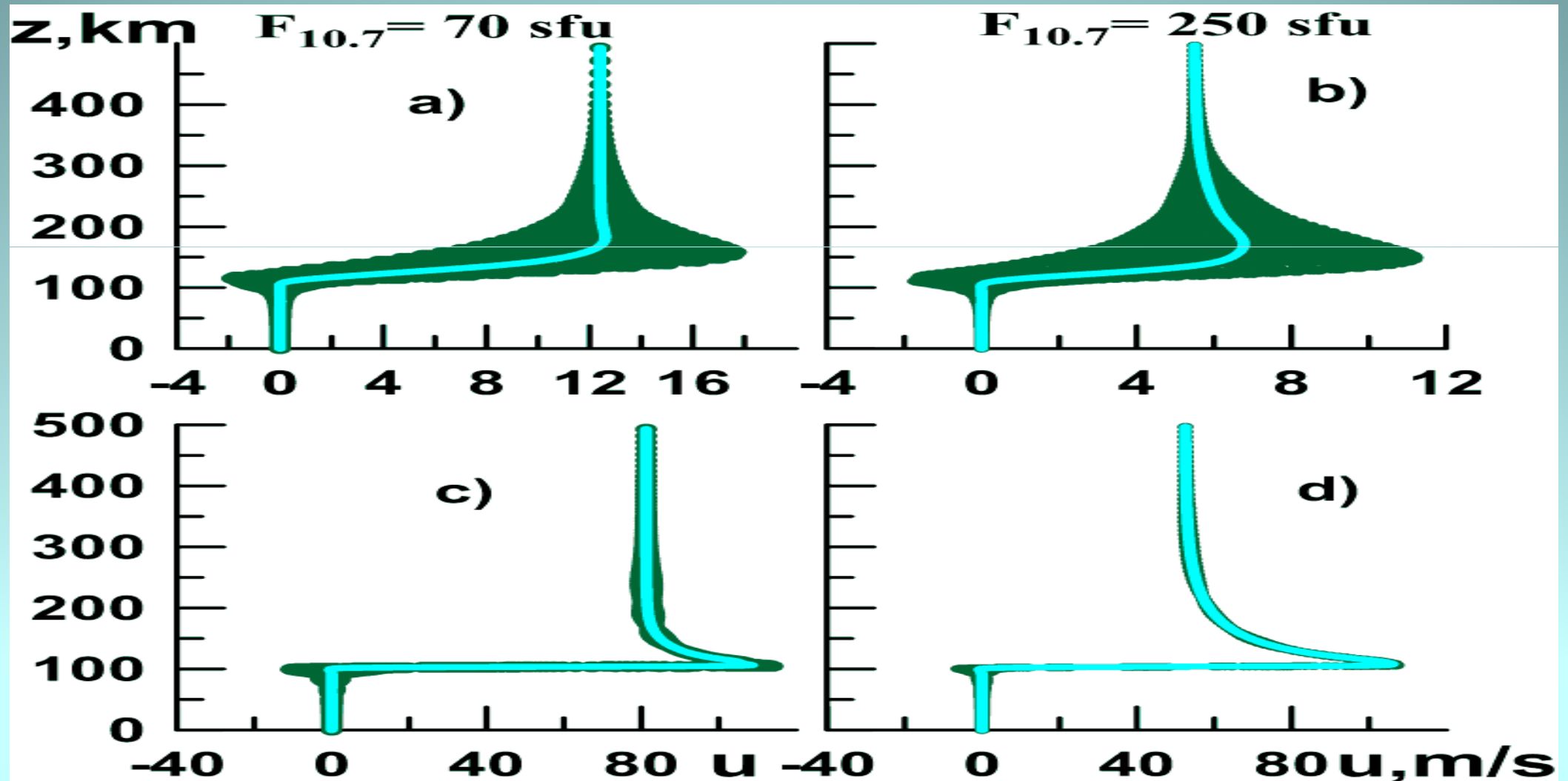


**Time variations of the temperature standard deviation at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.**

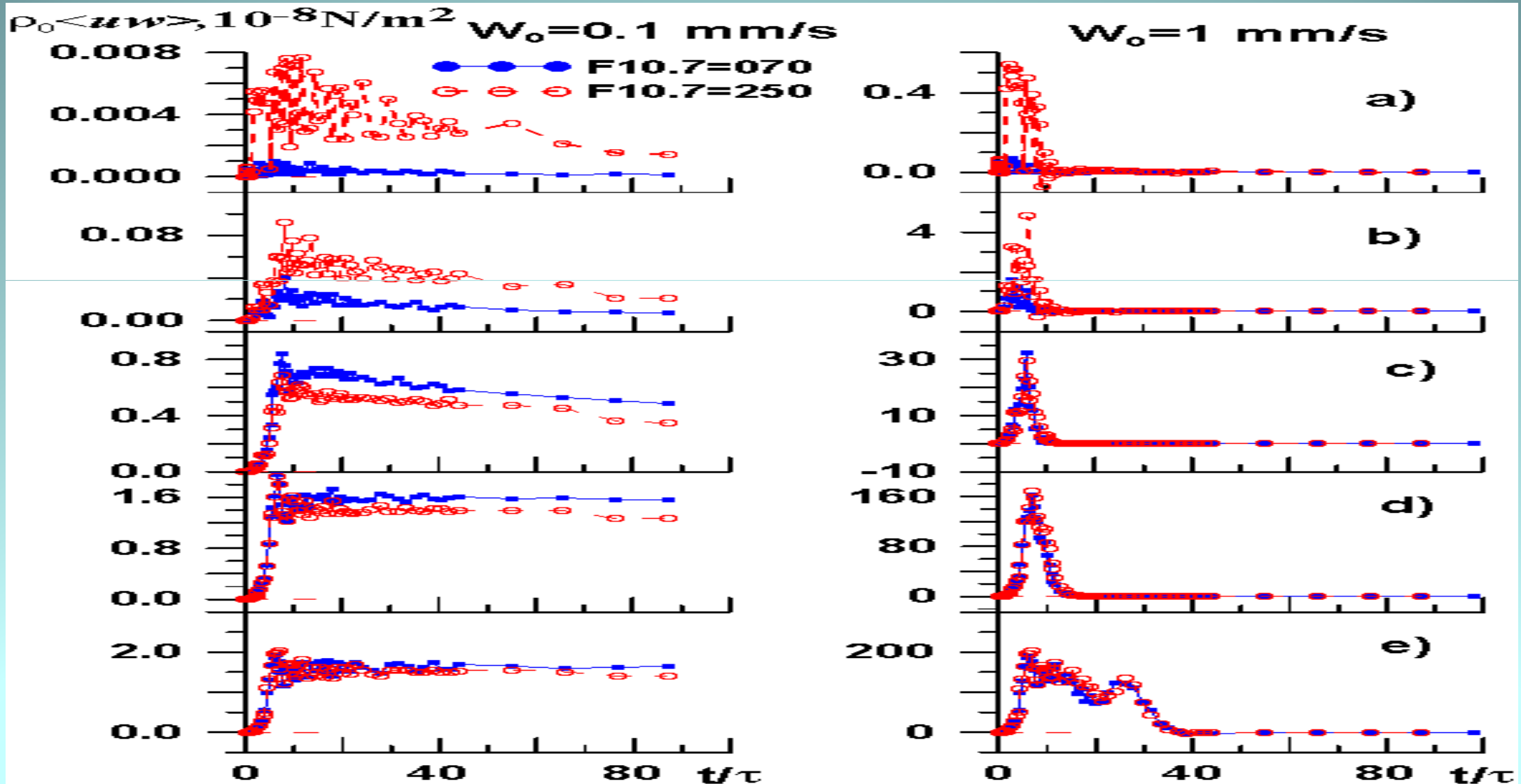


# **5. Wave-induced mean flows**

**Horizontal velocity perturbations from AGW source**  
with period  $\tau = 2 \times 10^3$  s and  $c_x = 100$  m/s and amplitudes  $W_0 = 0.1$  mm/s (a,b) and  $W_0 = 1$  mm/s (c,d) at time  $t = 55\tau$  for different values of solar radiowave flux ). Thick lines show average values for each altitude.

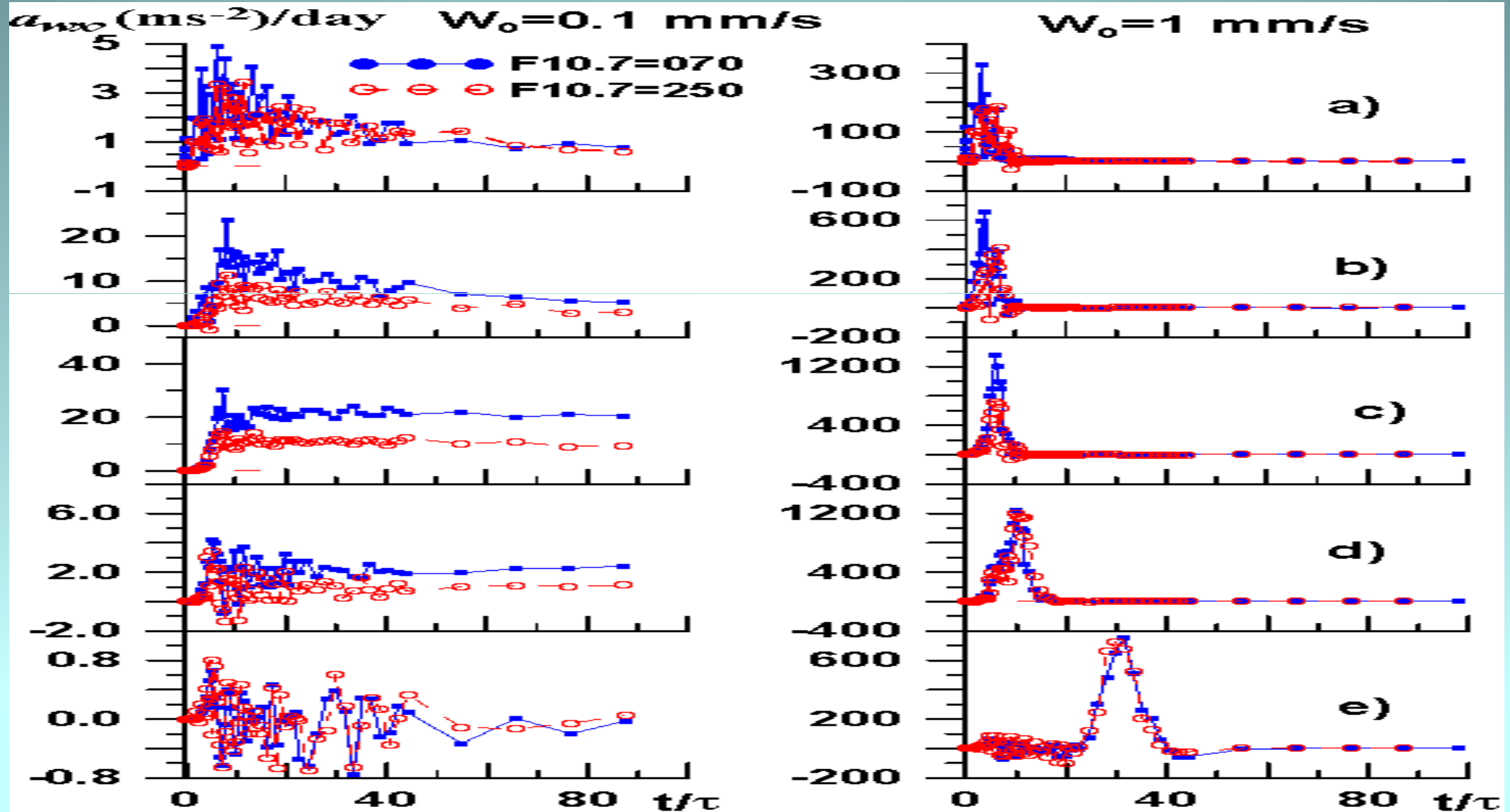


**Time variations of vertical wave flux of horizontal momentum**  
 at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity



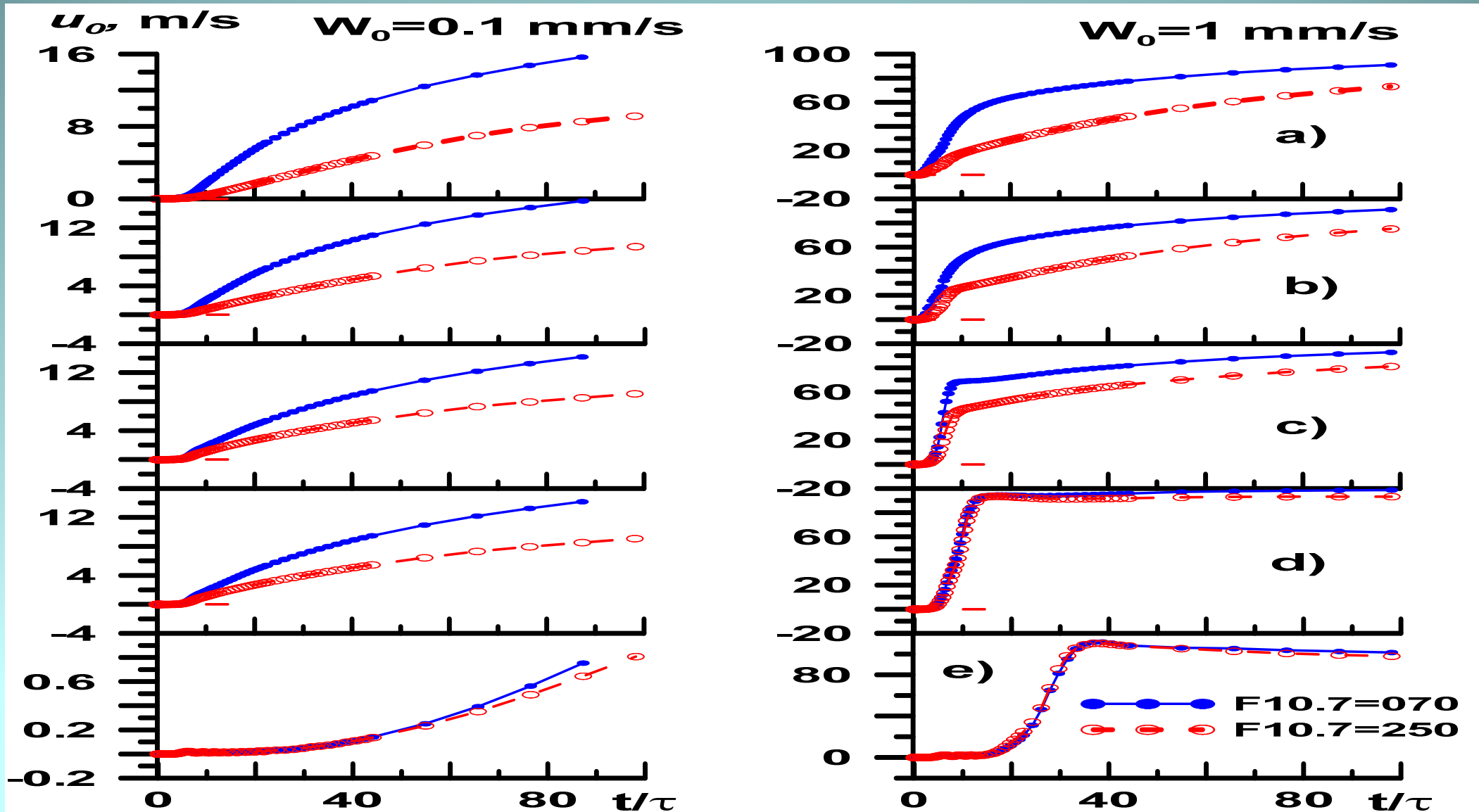
# Time variations of wave accelerations of the mean flow

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (left) and high (right) levels of solar activity.



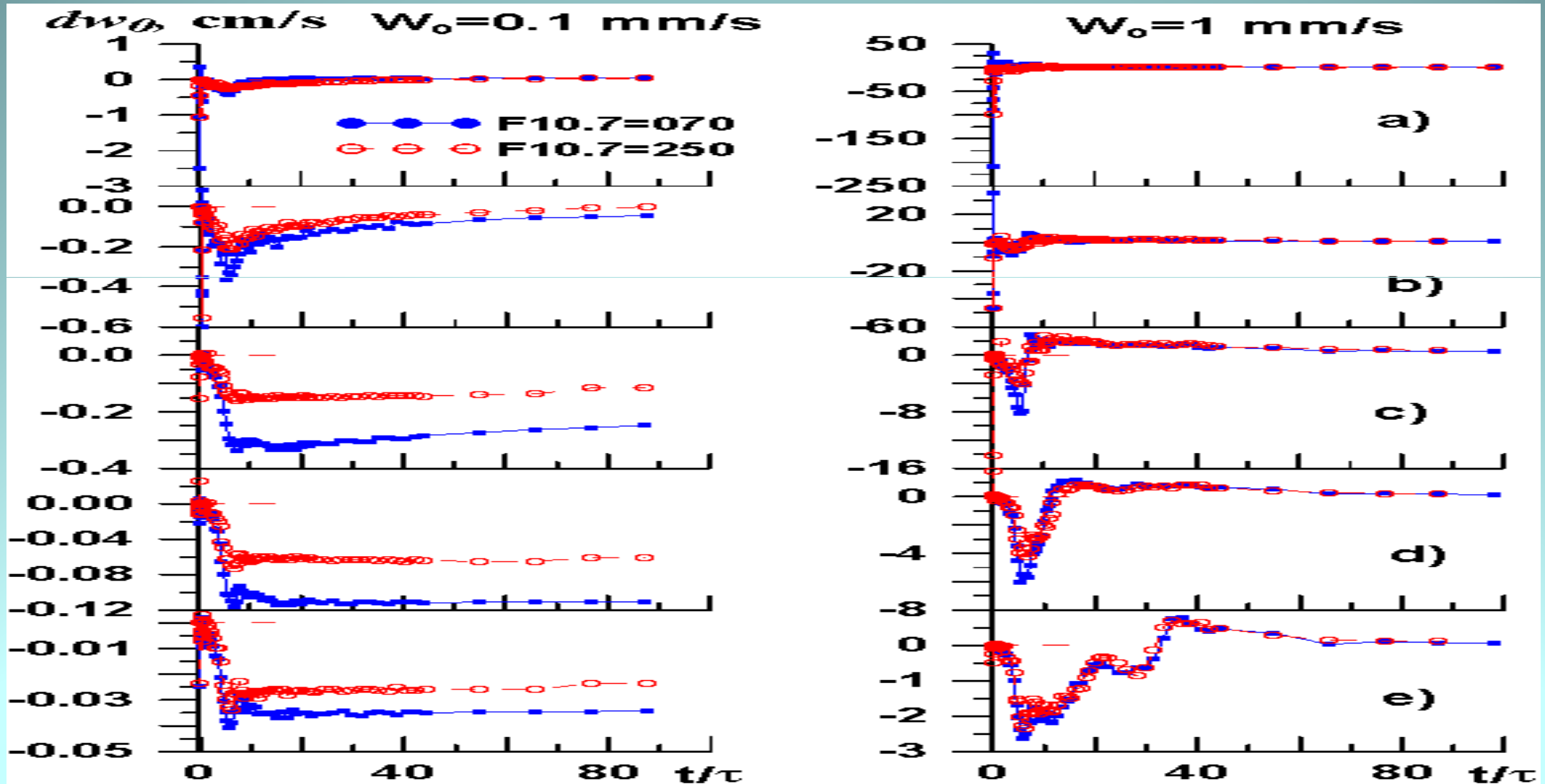
# Time variations of the mean horizontal velocity

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing (1) with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



# Time variations of the mean vertical velocity

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.

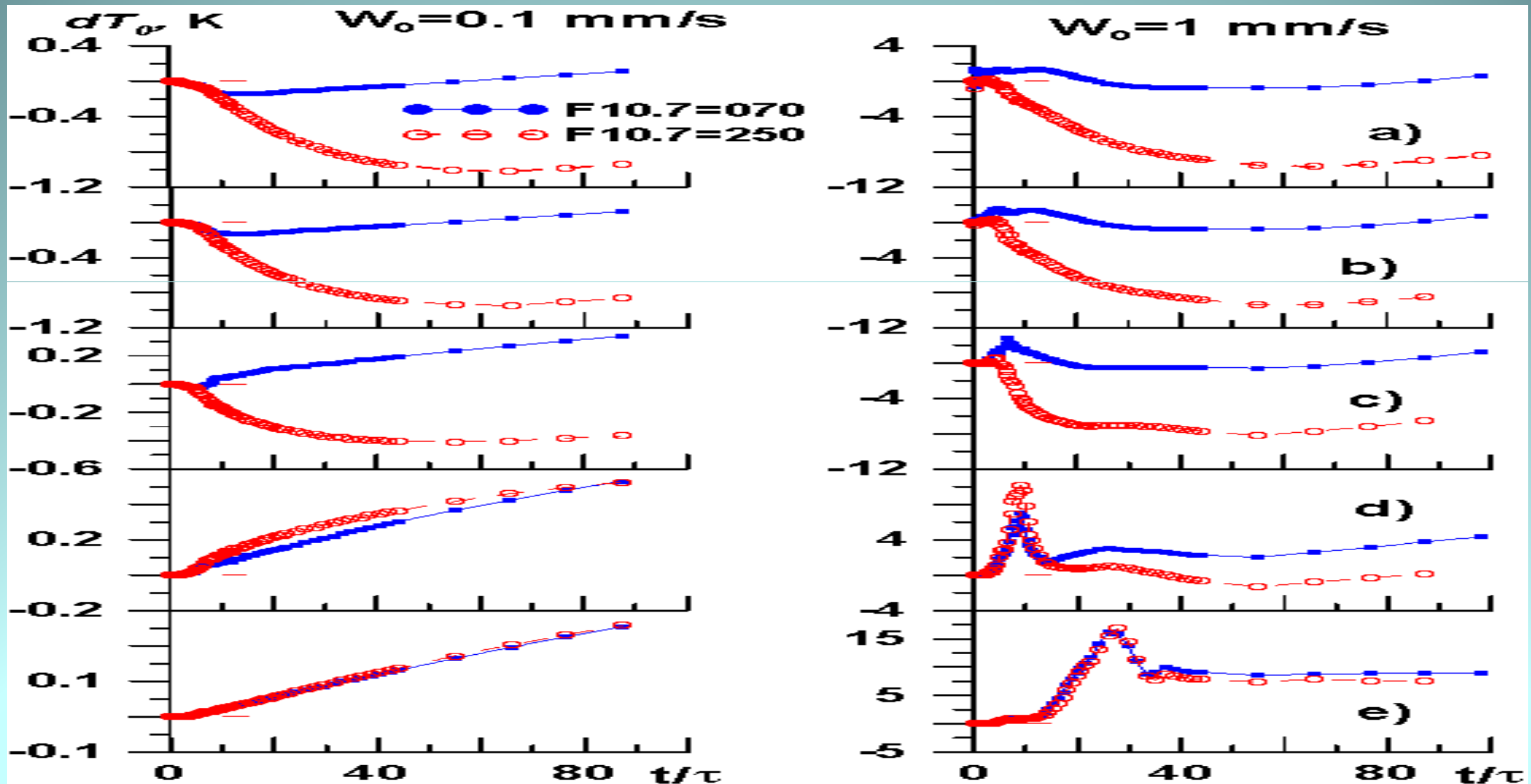




# **6. AGW thermal effect**

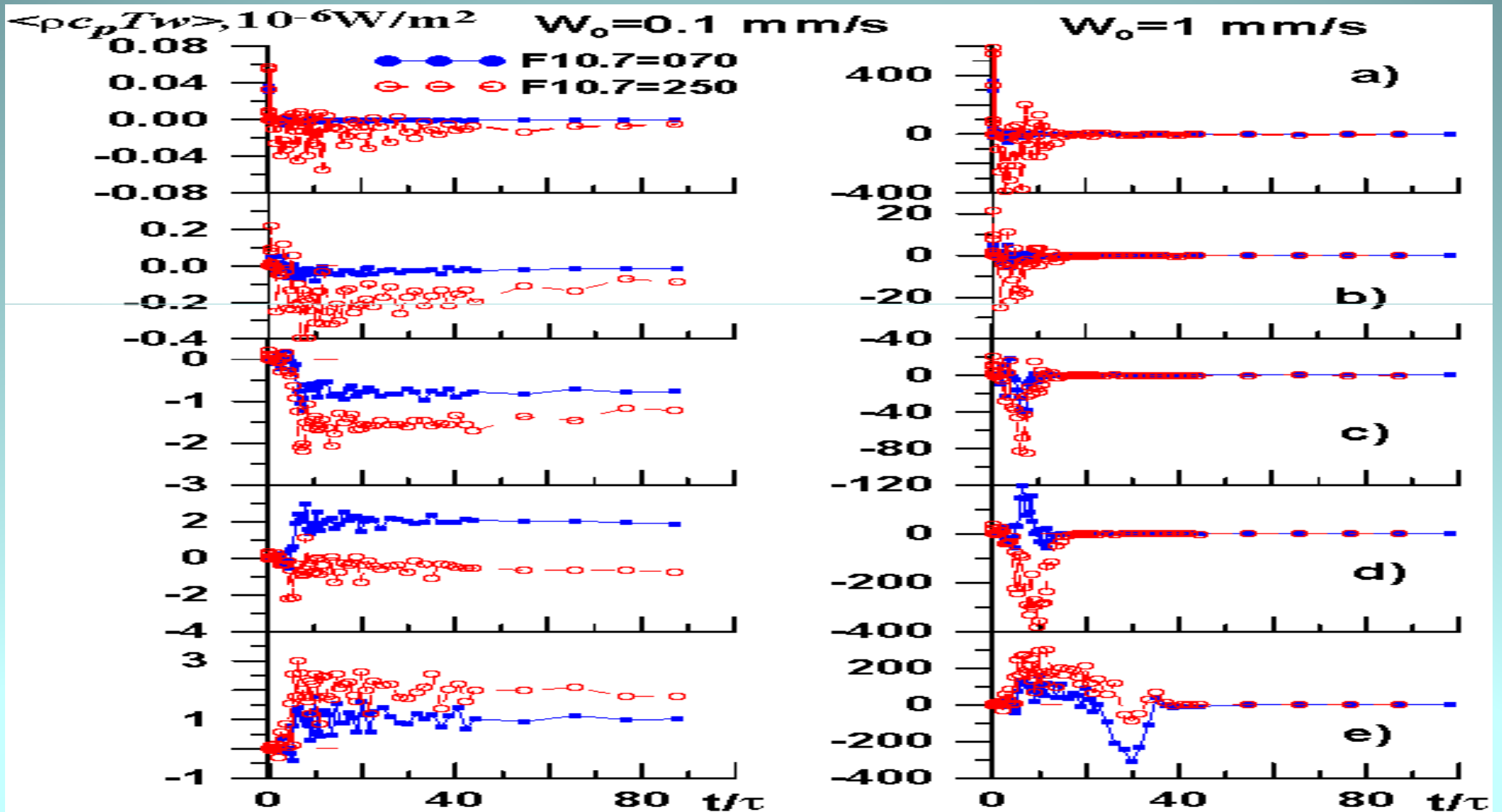
# Time variations of the mean temperature

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing (1) with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



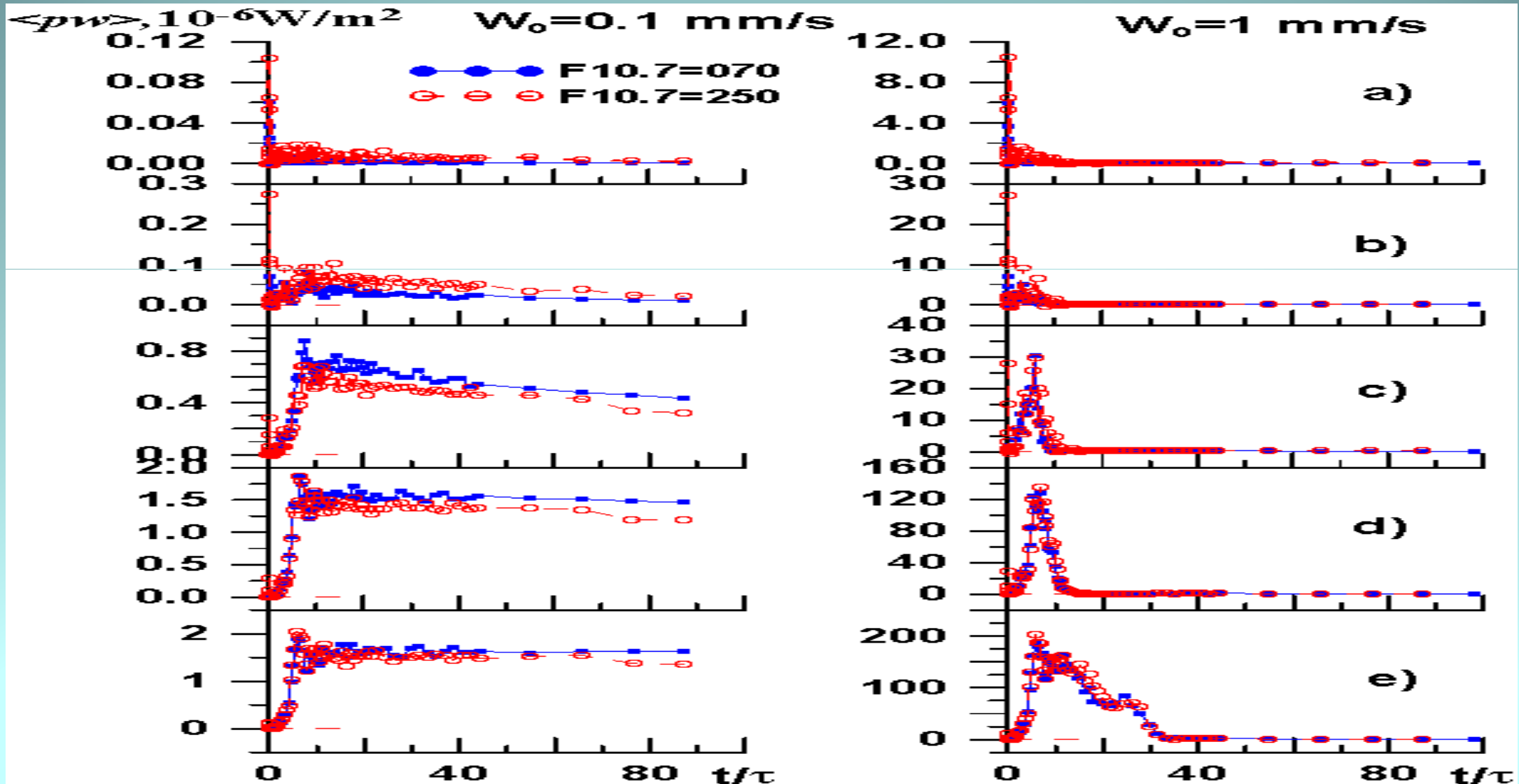
# Time variations of the wave heat flux

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing (1) with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



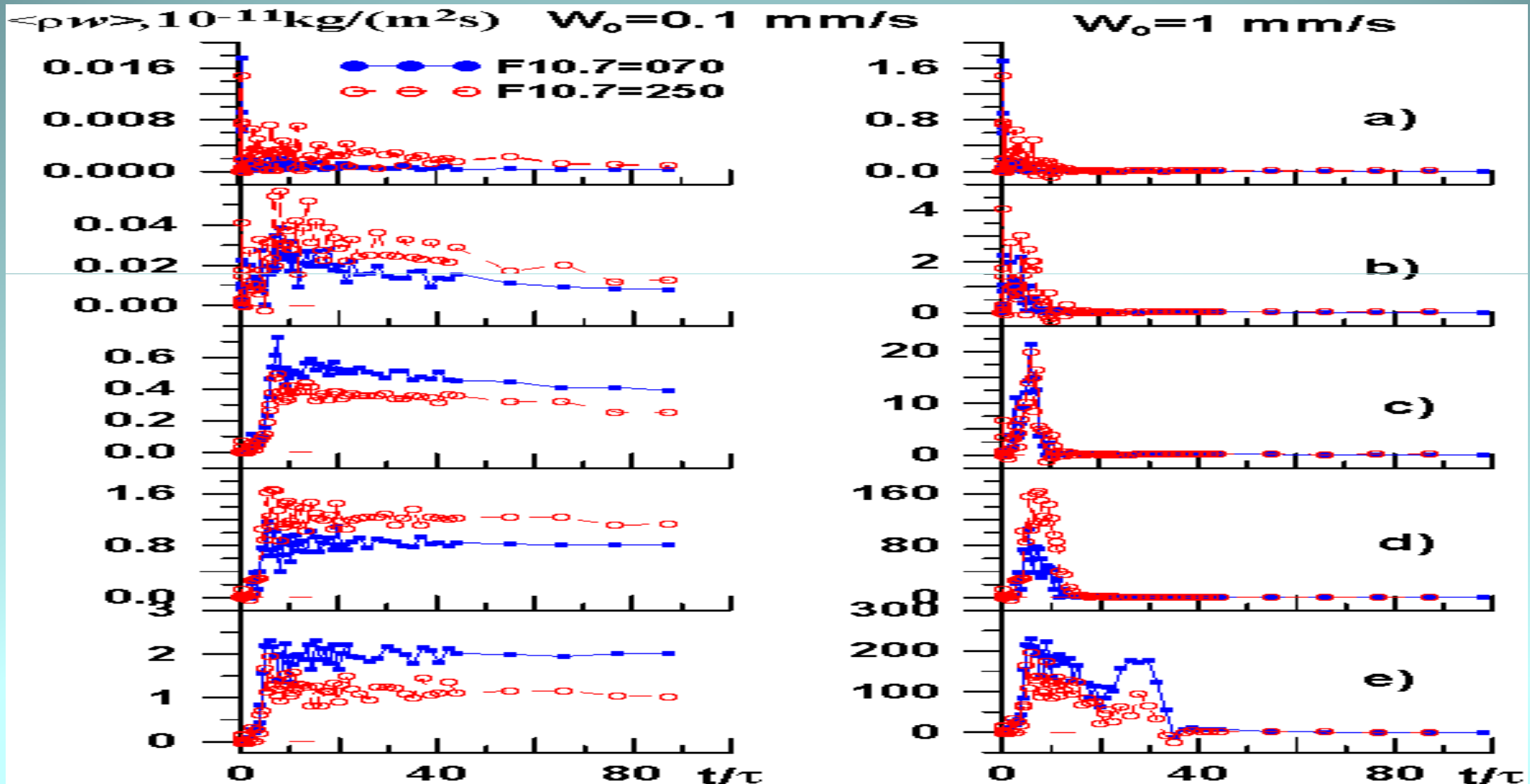
# Time variations of the wave energy flux

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



# Time variations of the wave mass flux

at altitudes 250 (a), 200 (b), 150 (c), 120 (d), 110 km (e) for amplitudes  $W_0 = 0.1$  mm/s (left) and  $W_0 = 1$  mm/s (right) of the surface wave forcing with period  $\tau = 2 \cdot 10^3$  s and  $c_x = 100$  m/s at low (blue) and high (red) levels of solar activity.



# Conclusion

- 1. Change in background temperature, density and molecular viscosity due to solar activity influences AGW characteristics, wave-induced jets and wave heating of the upper atmosphere.**
- 2. Wave accelerations and wave-induced jet streams are larger at lower solar activity.**
- 3. Above altitudes 150 km, IGWs produce heating at low solar activity and cooling at high solar activity.**
- 4. Numerical simulation of nonlinear AGW propagation helps better understanding the details of dynamical and thermal influence of waves coming from the troposphere on the mean temperature and wind in the middle and upper atmosphere.**